

2A.3. Composition of Functions

1 of 2

$$\boxed{\text{■}} \quad f(g(x)) \equiv f \text{ of } g \text{ of } x \equiv f \text{ composed with } g$$

$$\boxed{\text{■}} \quad g(f(x)) \equiv g \text{ of } f \text{ of } x \equiv g \text{ composed with } f$$

Example #1. For $f(x) = x^2 + 3x - 8$ and $g(x) = 4x - 7$, calculate

(a) $f(g(x))$ (b) $g(f(x))$ (c) $f(g(2))$ (d) $g(f(2))$

SOLUTION:

$$\begin{aligned} \text{(a)} \quad f(g(x)) &= f(g) = g^2 + 3g - 8 = (4x-7)^2 + 3(4x-7) - 8 = \\ &= (16x^2 - 56x + 49) + (12x - 21) - 8 = 16x^2 - 44x + 20 \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad g(f(x)) &= 4f - 7 = 4(x^2 + 3x - 8) - 7 = 4x^2 + 12x - 32 - 7 = \\ &= 4x^2 + 12x - 40 \end{aligned}$$

$$\text{(c)} \quad g(2) = 1, \quad f(g(2)) = f(1) = -4$$

$$\text{(d)} \quad f(2) = 2, \quad g(f(2)) = g(2) = 1$$

Example #2. Let $x \equiv$ list price of an item for sale.

(a) Write a function $f(x)$ which means \$10 off

(b) Write a function $g(x)$ which means 20% discount.

(c) Calculate $f(g(x))$ and state its meaning.

(d) Calculate $g(f(x))$ and state its meaning.

(e) Which is best for the customer, $f(g(x))$ or $g(f(x))$?

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2 of 2

SOLUTION:

(a) $f(x) = x - 10$ \leftarrow

(b) $g(x) = 0.8x$ \leftarrow

(c) $f(g(x)) = f(g) = g - 10 = 0.8x - 10$ \leftarrow

Take the 20% discount, then take \$10.00 off \leftarrow

(d) $g(f(x)) = 0.8f = 0.8(x - 10) = 0.8x - 8$ \leftarrow

Take \$10.00 off, then take the 20% discount.

(e) $f(g(x))$ is better \leftarrow