

AP CALCULUS AB

HOMEWORK #2

2.3. Discontinuity Types

Supplemental Problems:

1, 2, 3, 4

Section 2.3 Exercises, pg. 84

26¹, 30¹

2.3. Continuity

Supplemental Problems:

5, 6

Section 2.3 Exercises, pg. 84

47, 48

2.4. Average and Instantaneous Rates of Change

Section 2.4 Exercises, pg. 93

1, 3, 5, 10^{2,3}

2.4. Velocities

Section 2.4 Exercises, pg. 93

33⁴, 35^{3,4}

Supplemental Problems:

7^{3,5}

Notes:

1. Cancel out the hole.
2. The slope of the function at $x = 1$ is

$$m_T(1) = \lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h}.$$
3. Draw the graph on the grid provided.
4. The slope of the function, as a function of x , is

$$m_T(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}.$$
5. The velocity of the car, as a function of time, is

$$v(t) = \lim_{h \rightarrow 0} \frac{x(t+h) - x(t)}{h}.$$

Supplemental Problems:

For problems 1 through 4, state the discontinuity types and their x – locations.

1)

$$f(x) = \frac{2x^2 + 3x}{|x|}$$

2)

$$f(x) = \cos\left(\frac{2\pi}{x^2 - 4}\right)$$

3)

$$f(x) = \frac{5x + 3}{5x^2 + 33x + 18}$$

4)

$$f(x) = \frac{x + 3}{2x^2 + 13x - 7}$$

- 5) For $f(x) = x^2 - 8x + 17$ defined on $x \in [3, 7]$, find the value of $c \in (3, 7)$ guaranteed to exist via the IVTCF such that $f(c) = 6$. Verify that $f(3) < 6 < f(7)$.

6)

$$\lim_{x \rightarrow 8} (x^2 - 8x + 17) = ?$$

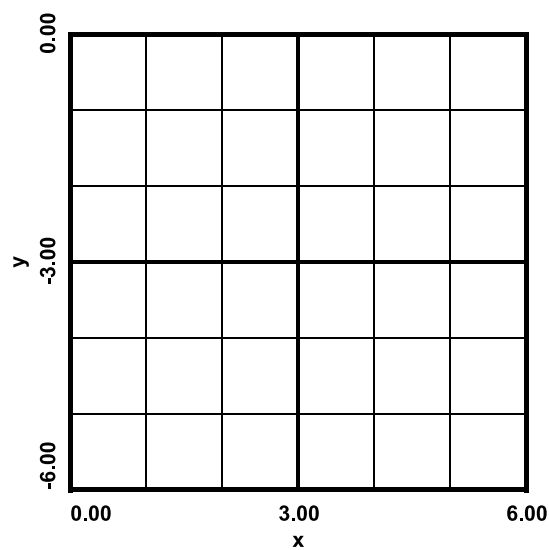
- 7) A car completes a 0.25 – mile (1320 ft) drag race in 6 seconds. The position x of the car (in feet), as a function of time (in seconds), is given by

$$x = \frac{22}{9}(21t^2 - t^3).$$

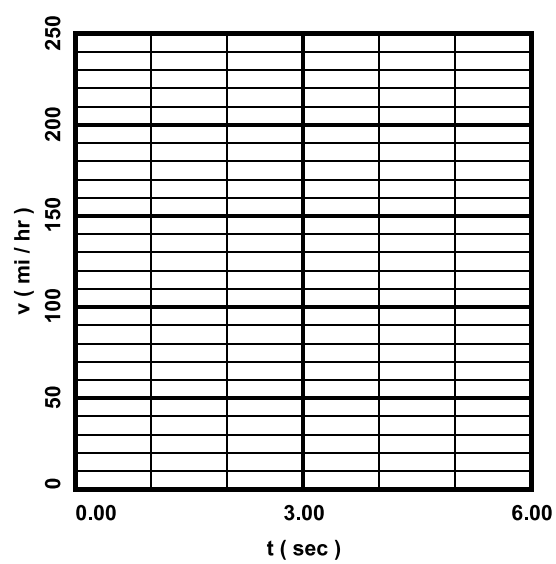
- a) Calculate the velocity of the car $v = v(t)$, where v is in ft/sec, and t is in seconds.
- b) Express your result from part **a** to have v being in mi/hr and t being in seconds.
- c) Graph $v = v(t)$ from part **b** on the grid provided.
- d) Calculate the maximum value of v , in mi/hr, which occurs during $t \in [0, 6]$ seconds.
- e) Calculate the average value of v over $t \in [0, 6]$ seconds in mi/hr.

Grids:

10)



7)



35)

